

Chaotic Rivest-Shamir-Adleman Algorithm with Data Encryption Standard Scheduling

Edwin R. Arboleda¹, Joel L. Balaba², John Carlo L. Espineli³

Department of Computer and Electronics Engineering, Cavite State University, Cavite, Philippines

*Corresponding author, e-mail: edwin.r.arboleda@cvsu.edu.ph¹, jbalaba26@gmail.com², johncarloespineli@gmail.com³

Abstract

Cryptography, which involves the use of a cipher, describes a process of encrypting information so that its meaning is hidden and thus, secured from those who do not know how to decrypt the information. Cryptography algorithms come with the various types including the symmetric key algorithms and asymmetric key algorithms. In this paper, the authors applied the most commonly used algorithm, which is the RSA algorithm together with the Chaos system and the basic security device employed in the worldwide organizations which is the Data Encryption Standard (DES) with the objective to make a hybrid data encryption. The advantage of a chaos system which is its unpredictability through the use of multiple keys and the secrecy of the RSA which is based on integer factorization's difficulty is combined for a more secure and reliable cryptography. The key generation was made more secure by applying the DES schedule to change the keys for encryption. The main strength of the proposed system is the chaotic variable key generator that changes the value of encrypted message whenever a different number of key is used. Using the provided examples the strength of security of the proposed system was tested and demonstrated.

Keywords: cryptography, encryption algorithm, chaos, RSA algorithm, Data Encryption Standard (DES)

1. Introduction

The most important concern in the current digital technology is the privacy and security of information. It is also one of the principal challenges of resource sharing on data communication network. Data security becomes critical especially when resources are being shared between computers.

Chaos system has been gaining popularity in the world of cryptography for its sensitivity to initial condition and its capability to generate apparently unpredictable behavior which make the system more complex and secure [1]. Chaotic systems have properties that created huge impact, such as the sensitive dependence on initial conditions and system parameters, pseudorandom property, no periodicity and topological transitivity, etc. Most properties meet some requirements such as diffusion and mixing in the sense of cryptography making chaotic cryptosystems to have more useful and practical applications [2–5]. Chaos functions aids in the development of mathematical models for nonlinear systems. The deterministic property of the chaos maps can make the system able to get the same set of values given there is exactly the same mapping function and initial value. But when there is a slight difference from the used initial value, it will cause a huge difference in the cipher-text produced using chaos. This makes the system to be secure from brute force attacks and it is difficult to make long term predictions on chaotic systems. Due to the properties of chaos system, recent researches of encryption algorithms have been increasingly based on chaotic systems [6–9].

RSA algorithm with a specific message block size allows a message sender to generate a public keys to encrypt the message and the receiver is sent a generated private key using a secured database. An incorrect private key will still decrypt the encrypted message but in a form different from the original message [10]. RSA is named after its inventors Ron Rivest, Adi Shamir and Leonard Adleman at MIT who first proposed a description of the algorithm publicly in 1977. It is a form of asymmetric cryptography. A user of RSA creates and then publishes a public key based on the two large prime numbers, along with an auxiliary value. The prime

numbers must be kept secret. Anyone can use the public key to encrypt a message, but with currently published methods, if the public key is large enough, only someone with knowledge of the prime numbers can feasibly decode the message [11]. RSA have many flaws in its design therefore not preferred for the commercial use. When the small values of the two large prime numbers, p & q are selected for the designing of key the encryption process becomes too weak and one can be able to decrypt the data by using random probability theory and side channel attacks. On the other hand if large p & q lengths are selected then it consumes more time and the performance gets degraded in comparison with DES. Further, the algorithm also requires of similar lengths for p & q, practically this is very tough conditions to satisfy. Padding techniques are required in such cases increases the system's overheads by taking more processing time [12]. RSA cryptography is a widely used encryption algorithm and is used in many different applications. [13–15]. Over the years a number of researches have enhanced the RSA or combined it with other algorithms to improve its security features [16–19].

The Data Encryption Standard (DES) has been the most extensively used encryption algorithm in recent times. The strength of DES is that decryption process can only be done by knowing the customized keys used in the encryption process. It uses the subkey rotation table by shifting number of bits indicated by the subkey index. It is the most widely used private key block cipher. It was first adopted in the year 1977 by the National Bureau of Standards as Federal Information Processing Standard 46 (FIPS PUB 46) [20-21].

In this paper, the authors proposed a hybrid cryptographic technique using RSA, Chaos System and DES scheduling concepts to provide more secure and reliable encryption algorithm. The shifting schedule of the DES gives an added complexity to the combined Chaos-based and RSA cryptosystem. The advantage of a Chaos system which is its unpredictability through the use of multiple keys and the secrecy of the RSA which is based on integer factorization's difficulty were combined for a more secure and reliable cryptography.

2. Research Method

2.1. RSA, Chaos, and DES Scheduling Cryptosystems

a. RSA Cryptosystem

Rivest-Shamir-Adleman (RSA) Algorithm, created and developed by Ron Rivest, Adi Shamir and Leonard Adleman at MIT in 1978, is the most widely used public key cryptosystem. It may be used to provide both secrecy and digital signatures and its security is based on the difficulty of the integer factorization. The RSA algorithm involves three steps: key generation, encryption and decryption [22].

- Key Generation

RSA involves a public key and a private key. The public key can be known to everyone and is used for encrypting messages. Messages encrypted with the public key can only be decrypted in a reasonable amount of time using the private key. The keys for the RSA algorithm are generated through the following ways:

- 1) To generate the two keys, choose two random large prime numbers (p) and (q). For maximum security, choose p and q of equal length. Compute the product $n=p \cdot q$
- 2) Then randomly choose the encryption key e such that e and $(p-1)(q-1)$ are relatively prime.
- 3) Finally, use the extended Euclidean algorithm to compute the decryption key (d) such that $d \equiv e^{-1} \pmod{(p-1)(q-1)}$. Note that d and n are also relatively prime.
- 4) The numbers e and n are the public key; the number d is the private key. The two prime numbers p and q are no longer needed. They should be discarded, but never revealed.

- Encryption

At first the receiver transmits her public key (n, e) to sender and keeps the private key secret. If sender wishes to send message M to receiver, sender changes the message M in to integer m, such that $0 \leq m < n$. Then sender computes the cipher text c corresponding to

$$c = m^e \pmod{n} \quad (1)$$

- Decryption:

Receiver can recover m from c by using her private key exponent d via computing

$$m = c^d \pmod{n} \quad (2)$$

2.2. Secure and Fast Chaos Cryptosystem

The chaos algorithm of this paper is based on the Secure and Fast Chaos [23]. The following are the steps involved in the key generation, encryption and decryption of the Secure and Fast Chaos:

Pi=Plain text

Ci=Cipher text

- **Key generation**

- a) Choose the values of parameter (M, A, Xn).
- b) Use the following equation to generate the pseudo random numbers.

For n=1 to j

$$X_{n+1} = \{A * X_n(X_n - 1)\} \bmod (256) \quad (3)$$

where; A=any integer (1, 2, 3,.....)

Xn=initial value of chaotic function which is 2, 3, 4,....., n.

j=Number of keys

X_{n+1} =keys K1, K2, K3,.....,Kj (after applying gray code on X_{n+1})

- c) Apply gray code on these random numbers which are generated from X_{n+1} to build up the keys K1, K2, K3,.....,Kj .
- d) Keys are represented in 8 bit binary form.

- **Encryption**

- a) Each character is shown in ASCII character, Pi=ASCII(character i).
- b) ASCII character Pi is converted into 8 bit binary form.
- c) Using the equation $E_k m (P_i) C_i$ for all $i > 0$, and $m=1$ to j for encryption, Where $E_k m (P_i)$ is bit wise XORing on plaintext Pi with single key Km.
- d) Find the 1's complement of ciphertext.

- **Decryption**

- a) Find the 1's complement of receiving ciphertext (Ci).
- b) Using the equation $P_i D_k m (C_i)$. Where $m=1$ to j for decryption, where $D_k m (C_i)$ is bit wise XORing on cipher text Ci with single key Km.
- c) Plain text Pi is converted into ASCII (Pi) with respect to its decimal value.
- d) Then Character i=ASCII (Pi).

2.3. DES Schedule for Keyshift

DES uses the subkey rotation table to split and shift number of bits as indicated by the subkey index [20] shown in Table 1.

Table 1. DES Rotation Table

Round number	1	2	3	4	5	6	7	8
<i>Rotate by</i>	1	1	2	2	2	2	2	2
Round number	9	10	11	12	13	14	15	16
<i>Rotate by</i>	1	2	2	2	2	2	2	1

3. Results and Analysis

3.1. Proposed Hybrid Algorithm

The proposed method is the combination of DES Schedule, Chaos and RSA cryptosystem. The shifting schedule of the DES gives an added complexity to the combined chaos-based and RSA cryptosystem. The advantage of a chaos system which is its unpredictability through the use of multiple keys and the secrecy of the RSA which is based on integer factorization's difficulty is combined for a more secure and reliable cryptography. Figure 1 shows the block diagram of the proposed algorithm.

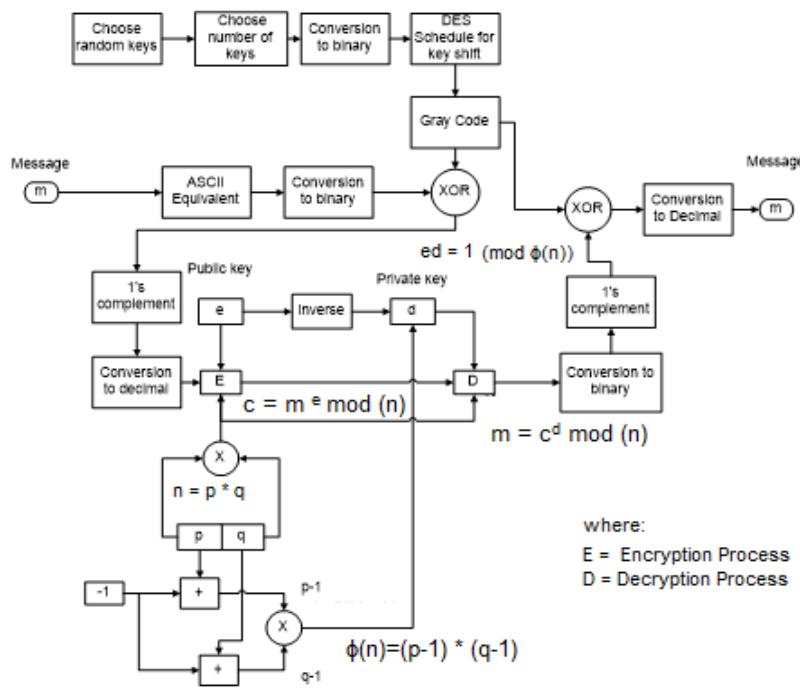


Figure 1. Block diagram of the proposed algorithm

Figure 1. is explained in the following processes:

- Key Generation

Steps:

1. Choose random number keys
2. Choose number of keys
3. Convert to binary
4. Use DES scheduling for key shift
5. Get the Gray code (this will be used to encrypt the message before RSA Encryption) Using the RSA Key Generation:
6. Choose p (prime number greater than any number in the message; $p > m$)
7. Choose q (any prime number)
8. Get $n = p * q$
9. Get $\phi(n) = (p-1) * (q-1)$
10. Choose value for e =(any prime number with no GCD with $\phi(n)$)
11. Get the value of d using Euclidean Algorithm

- Encryption

Steps:

Using Chaos encryption:

1. Get the decimal equivalent of ASCII
2. Convert decimal to binary
3. XOR message with corresponding g1 to g6
4. Get the 1's complement
5. Convert to decimal (this will be used for RSA encryption)
6. Get the cipher text by RSA Encryption using the formula:

$$c = m^e \text{ mod}(n)$$

- Decryption

RSA Decryption:

1. Get the value of m using the formula:

$m=c^d \bmod(n)$

2. Get the original messages using Chaos decryption:
3. Convert to decimal Get the decimal equivalent of ASCII
4. Get the 1's complement
5. XOR with corresponding g1 to g6
6. Convert binary to decimal
7. Get the ASCII equivalent

3.2. Example of the Proposed Hybrid Algorithm

Table 2, 3 and 4 shows the key generation, encryption and decryption of the proposed algorithm using the message below.

ASCII Equivalence: H=72, E=69, L=76, O=79

Table 2. Key Generation

STEP	PROCESS	RESULT
1	Choose random keys	$k_1=12, k_2=14, k_3=16, k_4=18, k_5=20$
2	Choose number of keys	5 keys
3	Conversion to binary	$12=0000\ 1100$ $14=0000\ 1110$ $16=0001\ 0000$ $18=0001\ 0010$ $20=0001\ 0100$
4	DES Schedule for key shift	$0001\ 1000$ $0001\ 1100$ $0100\ 0000$ $0100\ 1000$ $0101\ 0000$
5	Gray code	$0001\ 0100$ $0001\ 0010$ $0110\ 0000$ $0110\ 1100$ $0111\ 1000$
6	Choose p (prime number greater than any number in the message)	$p=127$
7	Choose q (any prime number)	$q=7$
8	Get $n=p \times q$	$n=127 \times 7=889$
9	Get $\phi(n)=(p-1) \times (q-1)$	$\phi(n)=126 \times 6=756$
10	Choose value for e=(any prime number with no GCD with $\phi(n)$)	$e=11$
11	Get the value of d using Euclidean Algorithm	Step 1: Euclidean Algorithm $e \times d = 1 \pmod{\phi(n)}$ $756=68(11)+8$ $11=1(8)+3$ $8=2(3)+2$ $3=1(2)+1$
		Step 2: Extended Euclidean Algorithm (Back Substitution) $1=3-1(2)$ $1=3-1[8-2(3)]$ $1=3-1(8)+2(3)$ $1=3(3)-1(8)$ $1=3[11-1(8)]-1(8)$ $1=3(11)-3(8)-1(8)$ $1=3(11)-4(8)$ $1=3[11]-4(756-68(11))$ $1=3(11)-4(756)+272(11)$ $1=275(11)-4(756)$ Use d=275 since it is already a positive number $d=275$

Note: The complete instruction on how to get d can be found in [24]

Table 3. Encryption

STEP	PROCESS	RESULT	
		Message	ASCII
1	Convert message into ASCII equivalent	H E L L O	72 69 76 76 79
2	Convert ASCII equivalent into Binary	01001000 01000101 01001100 01001111 01011100 01010111	
3	Message in binary \oplus Gray code (g_n)	00101100 00100000 00110111 10100011 10101000	
4	Get the 1's complement	11010011 11011111 11001000 163	
5	Convert to decimal (this will be used for RSA encryption)	168 211 223 200	
6	Get the cipher text by RSA Encryption using the formula: $c=m^e \bmod (n)$	648 875 15 118 856	

Table 4. Decryption

STEP	PROCESS	RESULT
1	Get the value of m using the formula: $m=c^d \bmod (n)$	163 168 211 223 200 10100011
2	Convert to decimal Get the decimal equivalent of ASCII	10101000 11010011 11011111 11001000 01011100 01010111
3	Get the 1's complement	00101100 00100000 00110111 01001000 01000101
4	XOR with corresponding g1 to g6	01001100 01001100 01001111 ASCII 72
5	Convert binary to decimal	69 76 76 79
6	Get the ASCII equivalent	Message ASCII H 72 E 69 L 76 L 76 O 79

3.3 Analysis of the Proposed Method

3.3.1. Sensitivity to Number of Keys

It is claimed by the proposed method that if number of keys are changed, then the cipher texts completely changed from one another for same plain text.

Table 5. Sensitivity of Number of Keys of the Proposed System

Message	No. of keys	Public keys e=11 n=889	Private keys n=889	Ciphertext
HELLO	1	k=12 g1=0001 0100 k=12,14	d=275	648,419,839, 839,607
HELLO	2	g1=0001 0100 g2=0001 0010 k=12,14,16	d=275	648,875,232, 821,181
HELLO	3	g1=0001 0100 g2=0001 0010 g3=0001 0000 k=12,14,16,18 g1=0001 0100	d=275	648,875,15, 232,71
HELLO	4	g2=0001 0010 g3=0001 0000 g4=0001 0010 k=12,14,16,18,20 g1=0001 0100	d=275	648, 875, 15, 118,122
HELLO	5	g2=0001 0010 g3=0001 0000 g4=0001 0010 g5=0001 0100	d=275	648,875,15, 118, 856

Table 5 shows the effect of using different keys in the generation of cipher text. It can be observed that a change in the number of keys would also result to a change in the generated cipher text. In the message “HELLO”, when only one key is used, the letter “L” has the same cipher text. But when using two or more keys, the message “L” generates different cipher text which makes it more advantageous and difficult to be deciphered by the attackers because it will be a mystery on how many keys did the sender used.

3.3.2. Security Analysis

Changing one bit in the plaintext or one bit in the key changes the bits in the cipher text [25]. Using two different keys also produces different cipher text given the same data information [26]. This makes the system harder to decipher when trying to come up with an attack. This important characteristic of an encryption algorithm is called the avalanche effect [27].

Multiple keys k and one private key d were used in table 4 to encrypt the message. Another implementation of the proposed method is use not only one random number k but multiple k's for encryption.

Table 6. The Avalanche Effect of the Proposed System using One K and Multiple K

Message	Parameters	Random number	Cipher text
blowzy night-	p=127		737,32,487,27,815,419,
frumps vex'd jack	q=7		11,12,744,883,389,648
q	n=889	k1=12	633,809,569,101,624,232,
	e=11		191,11,35,40,182,557,131
	d=275		11,525,705,829,76,11,518
blowzy night-	p=127	k1=12	737,340,557,212,253, 419
frumps vex'd jack	q=7	k2=14	272,299,27,693,389,870
q	n=889	k3=16	40,299,819,9,382,389,693
	e=11	k4=18	839,35,246,84,829,839,11
	d=275	k5=20	809,110,210,150,11,858

In Table 6, the proposed system was implemented in two different ways. The same message was encrypted using same prime number, public keys and private key. The only difference is in the number of k and values of k used. It can be observed that the encrypted message greatly differs from one another. In Tables 5 and 6, the avalanche effect was demonstrated by the proposed method on the number and values of random numbers used.

4. Conclusion

The proposed system was able to combine the secure and fast chaos cryptosystem, DES scheduling and the RSA cryptosystem. It is a combination of the multiple keys of chaos system and the strength of the RSA algorithm by having multiple keys as in the concept of the chaos cryptosystem in able to have different cipher text for encryption. The key generation was made more secure by applying the DES schedule to change the keys for encryption. The proposed method provided for the RSA cryptosystem's way of manipulating random numbers used to create an avalanche effect in the produced cipher text. The chaotic properties of the proposed system lie in the number of random numbers used. The system successfully proved the important characteristics of the proposed hybrid system in the encryption of data in a more secure way.

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